

## FAST IMPLEMENTATION OF HOMOMORPHIC FILTERS FOR IMAGE ENHANCEMENT

### Background of the Invention

The present invention relates to the digital image processing arts. More particularly, the present invention relates to a method for fast implementation of homomorphic filters to enhance digital images that have strong local imbalances in exposure. The subject invention differs significantly from conventional homomorphic filtering in that low-pass filtering is used to derive or estimate an image that represents the light source in an input image. This low-pass lightsource image is used to derive an enhanced version of the input image wherein the influence of the lightsource is dampened.

Homomorphic filters are well known and used in digital image enhancement and restoration to eliminate or at least attenuate strong local imbalances in exposure. Such exposure imbalances occur, for example, when a first portion of an object featured in an image is strongly illuminated, and a second portion of the object is hidden in a dark shadow. Such an image is sub-optimal and it has been deemed highly desirable to enhance the image so that the object appears more evenly illuminated. Homomorphic filters are described, for example, in the following references that are hereby expressly incorporated by reference: (i) Gonzales and Woods, Digital Image Processing, p213ff, Addison Wesley 1993, ISBN 0-201-50803-6; and, (ii) Ekstrom, Digital Image Processing Techniques, p41ff, Academic Press 1984, ISBN 0-12-236760-X.

Homomorphic filters are based upon the assumption that the light distribution in a recorded image is defined by a multiplication of the reflectance of the objects and the scene illumination, i.e., image  $(i) = \text{light}(l) * \text{object}(o)$ . Taking the logarithm, this can be expressed in the density domain as  $\ln(i) = \ln(l) + \ln(o)$ , thereby creating a new image description, where the illumination can be

expressed using the formalism of "additive noise". Assuming that the illumination is low-pass or low-frequency with regard to the object, itself, one can perform a high-pass or band-pass filtering operation to dampen the effects of the illumination without noticeably impacting the object appearance. However, to be effective, the filter must extend over the entire image, since the illuminant variation extends over the entire image. At modern image resolutions of 300 or 600 dots per inch (dpi) or more, this filtering operation amounts to fast Fourier transforms FFT's of sizes 1000 x 1000 to 6000 x 6000 pixels, keeping in mind that the resolutions might further increase due to technology advances. The state of the art approach to homomorphic filtering cannot presently be implemented efficiently in printing and copying environments.

Standard homomorphic filters operate in line with the foregoing description. It is assumed that the image contains multiplicative contributions from the objects in the scene and the illumination according to:

$$i(x,y) = o(x,y) * l(x,y), \quad (1)$$

where  $o(x,y)$  represents the object and  $l(x,y)$  the lightsource. The intention of homomorphic filtering is to divide the lightsource out of the equation. To do this, one must have a good understanding of the unknown lightsource. A good assumption is the low-pass nature of the light source, and this forms the basis for homomorphic filters. In essence, the homomorphic filter divides the image by a low-pass version of same. Using logarithms, this can be expressed as follows:

$$\ln(i) = \ln(o) + \ln(l) \quad (2)$$

to which a high-pass or band-pass filter  $h$  is applied, giving a new output image  $i'$  according to:

$$\ln(i') = h \otimes \ln(o) + h \otimes \ln(l) \quad (3)$$

Assuming the lightsource component  $l$  has low frequency characteristics,  $\ln(l)$  also has low frequency characteristics. A properly designed filter would  $h$  would dampen the effect of the illumination in the image with respect to the object.

Since the illumination is assumed to have low-pass characteristics, the filter needs to be high-pass or band-pass with sufficiently large spatial support to cover the variations of the illuminating lightsource. This leads to the common implementation of the above equation by way of a Fourier transform and multiplication with  $H$  according to:

$$FT\{\ln(i')\} = H * FT\{\ln(o)\} + H * FT\{\ln(l)\} \quad (4)$$

which allows filters that cover the entire image size. It should be noted that it is the need of a large filter support that is driving the frequency domain implementation, rather than dividing the data of the image by its low-pass part.

Using the assumption

$$0 \approx |H * FT\{\ln(l)\}| \ll |H * FT\{\ln(o)\}| \approx |FT\{\ln(o)\}|$$

leads to

$$i'(x,y) \cong e^{h \otimes \ln(o(x,y))} \quad \text{or} \quad i'(x,y) \cong o(x,y) \quad (5)$$

This, in turn, shows that the homomorphic filter has effectively divided the lightsource contributions out of the image. It should be clear that certain contributions of the lightsource are still in the image, whereas certain contributions of the object are no longer present, based upon the quality of the filter choice.

Although homomorphic filtering can have a strongly positive impact on perceived image quality, the need to Fourier transform and filter large images and thus the relatively slow processing throughput, has negatively impacted its uses. Standard techniques to increase the speed processing such as sub-sampling can not be applied for morphological filtering. The reason is that the result of the filtering is a high pass version of the input. In sub-sampled image processing, the sub-sampled result needs to be up-sampled to get the final result. Up-sampling of high pass data is extremely unreliable and noise sensitive. Consequently, common sub-sampling techniques can not be applied in the described method.

In light of the foregoing deficiencies and others associated with conventional implementation of homomorphic filters, a need as been identified for a new and improved method for fast implementation of homomorphic filters for image enhancement.

#### **Summary of the Invention**

In accordance with the present invention, a method for simulating the effect of a homomorphic filtering operation to enhance an input image includes receiving input data that define an input image. Lightsource data that represent an image of the lightsource in the input image are derived from the input image. Enhanced data that represent an enhanced image are derived by removing the effect of the lightsource data from the input data. The lightsource data are preferably derived by sub-sampling the input data, low-pass filtering the sub-sampled image, and interpolating the low-pass filtered image to full-scale. The effects of the lightsource data are removed from the input data by a division operation or by subtraction in the density domain.

In accordance with another aspect of the present invention, an input image is received that has an illumination component and an object component. The input image is sub-sampled to obtain a subsampled image. The



homomorphic filters for image enhancement in accordance with the present invention;

FIGURE 2 is a flow chart that discloses a method for fast implementation of homomorphic filters for image enhancement in accordance with the present invention;

FIGURE 3 is a more detailed flow chart disclosing the method of FIGURE 2.

### **Detailed Description of the Preferred Embodiment**

Referring now to the drawings wherein the showings are for purposes of illustrating a preferred embodiment of the invention only and not for limiting the invention in any way, FIGURE 1 diagrammatically illustrates an image processing apparatus adapted for implementing a method for fast implementation of homomorphic filters in accordance with the present invention. In this example, the image processing apparatus comprises an image input terminal **12**, an image processing unit **14**, and an image output terminal **16**. The input terminal can be any source of digital image data including a scanner or a source of stored image data. The image processing unit (IPU) is provided by any suitable electronic computing apparatus including a microprocessor or the like for carrying out digital image processing as described herein. Image data from the input terminal **12** are supplied to the IPU **14** for processing. After processing the data, the IPU **14** outputs the data to the image output terminal **16** that comprises a non-impact printer, video display, image storage device or the like. Suitable image processing apparatus including an input terminal **12**, an image processing unit **14** and an image output terminal **16** are provided by digital xerographic image processing apparatus such as XEROX DocuTech document reproduction system or a conventional computer including a scanner, and a printer operatively connected thereto.

With the above-noted deficiencies of conventional homomorphic filtering in mind, the present invention is directed to a method that utilizes a low-pass filter rather than a high-pass or band-pass filter to separate the image of the object from the image of the lightsource. Use of a low-pass filter is critical so that filtering can be performed safely on a subsampled image, and wherein the filtered image can be up-interpolated to derive a full-scale image. Thus, according to the present invention, an intermediate function with low-pass characteristics is created, so that it may be safely up-interpolated to derive a full scale image of the lightsource.

In the preferred embodiment, this is accomplished by a filter  $H'$  that is equal to the inverse of the filter  $H$  described above, i.e.,  $H' = 1-H$ . Using this new filter, equation (4) above is rewritten as:

$$FT\{\ln(i')\} = (1-H) * FT\{\ln(o)\} + (1-H) * FT\{\ln(l)\} \quad (4a)$$

Since the filter  $H$  was said to be high-pass or band-pass, the new filter  $H'$  is low-pass, and the following relationship holds:

$$|FT\{\ln(l)\}| \approx |H * FT\{\ln(l)\}| \gg |H * FT\{\ln(o)\}| \approx 0$$

Those of ordinary skill in the art will recognize that this is the reverse relationship to that associated with conventional homomorphic filters as described above. This, then, leads to a change in equation (5) above so that:

$$i' \cong e^{h \otimes \ln(l)} \quad \text{or} \quad i' \cong l \quad (5a)$$

Equation 5 represents the homomorphic approximation of the light source. The main difference between eqs.(5) and (5a) is that eq.(5) attempts to approximate the object signal, a high pass signal, whereas eq.(6) attempts to approximate the

light source signal, a low pass signal, from the recorded image signal  $i$ . In this case,  $i'$  has low-pass characteristics and can easily be interpolated using standard up-sampling methods. In contrast to eq.(5), eq.(5a) does not yet represent the final output of the method. The final output is then obtained by:

$$i'' = i/i' = o \cdot I/i' = o \quad (6)$$

Thus, it can be seen that the image  $i''$  corresponds to the original image  $i$  or ( $o \cdot I$ ) divided by the lightsource image  $i'$  which results in the image of the object  $o$ , which is the desired output of a homomorphic filtering operation. It should be noted that the low pass characteristics of  $i'$  also allow the prevention of singularities in eq.(6) by enforcing  $i' > 0$ .

The method for fast implementation of homomorphic filters in accordance with the present invention is disclosed generally in FIGURE 2. Those of ordinary skill in the art will recognize that the method is suitable for enhancing digital images wherein a strong shadow is present and obscures a portion of the object(s) intended to be shown.

The method comprises a step **S1** of receiving image data defining an input image  $i$  in need of homomorphic filtering. A step **S2** subsamples the image data defining the input image so that image data defining a subsampled image is obtained. By definition, the subsampled image is smaller in size than the input image and, thus, is more suitable for high-speed processing as required in a printing, digital photography, or xerographic environment. The step **S2** can be accomplished according to any suitable subsampling operation with or without a prefiltering step. Where processing speed is critical, it is most preferred that the data defining the input image be directly subsampled without a prefiltering operation. This can generally be done safely without loss of critical image information owing to the fact that the subsampled image is later low-pass filtered as described below.



A step **S3** processes the subsampled image to extract or derive data that define an image of the lightsource from the subsampled image. At this stage, the image of the lightsource is equal in size to the subsampled image. Thus, a step **S4** is carried up to derive data that represent a full-scale image  $i'$  of the lightsource, i.e., an image of the lightsource that is equal in size to the input image.

A step **S5** uses the data defining the full-scale image  $i'$  of the lightsource to operate on the data that define the input image  $i$  to attenuate the effect of the lightsource in the input image  $i$ , i.e., to output the image  $i'' = o$ .

Referring now to FIGURE 3, a preferred embodiment of the foregoing method is described in further detail. The data defining the input image  $i$  are received **S1** and subsampled **S2** as described above. To implement the step **S3** of obtaining image data defining an image of the lightsource from the subsampled image, steps **S3a-S3c** are preferably implemented. The step **S3a** comprises performing a Fourier transform to move the image data defining the subsampled image into the frequency domain. A step **S3b** low-pass filters the subsampled frequency domain image data, and a step **S3c** transforms the low-pass filtered data back to the spatial domain. The steps **S3a-S3c** can be replaced by a step of low-pass filtering the subsampled image in the spatial domain. However, owing to the fact that the low-pass filter preferably spans the entire image to properly obtain an output image of the light source, those of ordinary skill in the art will recognize that processing in the frequency domain is generally preferred.

The step **S4** of deriving image data defining a full-scale image  $i'$  of the lightsource preferably comprises a step **S4a** of interpolating the image data defining the filtered, subsampled image. Although any interpolation method (e.g., nearest neighbor) may be used, it is preferred that the resulting full-scale image be low-frequency. Thus, it is most preferred to interpolate using a normal linear

interpolation or other low-order interpolation method as opposed to a high-order polynomial interpolation scheme.

The step **S5** of using the image data defining the full-scale image of the lightsource  $i'$  to attenuate the effect of the lightsource in the input image  $i$  is preferably carried out by a step **S5a** that comprises dividing the image data defining the input image  $i$  by the data defining the lightsource image  $i'$ . Of course, this has the same effect of a subtraction of the image  $i'$  from the image  $i$  in the density (logarithmic) domain. Alternatively, the full size approximation of the light source  $I$  can be used in eq.(2) after transforming both  $i$  and  $I$  into the logarithmic domain, followed by subtraction and reverse transform. The result of the step **S5a** is image data defining the image  $o$  of the object.

Modifications and alterations will occur to those of ordinary skill in the art to which the invention pertains upon reading this specification. It is intended that all such alterations and modifications fall within the scope of the invention as defined by the following claims as construed literally or according to the doctrine of equivalents.